# VITEEE 2021 Solutions May 31 - Slot 3

Q: A person is trying to move a 500 N caret across the level floor. To start the crate moving he has to pull it with a 230 N horizontal force. Once the crate starts to move it will move with constant velocity presence of an applied horizontal force. What is the coefficient of static friction.

- 1. 1.78
- 2.17.90
- 3.0.48
- 4. 1.80

#### Solution.

To solve the first question:

# Given:

- Weight of the crate, \( W \) = 500 N
- Force required to start the crate moving, \( F \) = 230 N
- The crate is on a level floor, so the normal force \( N \) is equal to the weight \( W \) of the crate.

The coefficient of static friction \( \mu\_s \) is given by: \[ \mu\_s = \frac{F\_{static}}{N} \] where \( F\_{static} \) is the static frictional force.

Given that a 230 N force is required to just start the crate moving,  $\$  {static} \) = 230 N.

So, \[ \mu\_s = \frac{230 N}{500 N} = 0.46 \]



None of the options provided match this answer. There could be a slight error or approximation used in the provided options, so the closest value to the calculated one is 0.48.

Answer for the first question: 3. 0.48

Q: The probability that both the pairs of twins are boys equals 0.32 and the probability of them being girls equals 0.32. Given one of them is a boy, the conditional probability that both twisna re boys is given by: Q:  $\varphi(x) = \varphi'(x)$  and  $\varphi(1) = 2$ , then  $\varphi(\log x)$  equals to:

- 1. 2/e
- 2. 1/e
- 3. x/e
- 4. 2x/e

# Solution.

\*\*For the first question:\*\*

# Given:

- Probability both pairs of twins are boys, \( P(BB) = 0.32 \).
- Probability both pairs of twins are girls, \( P(GG) = 0.32 \).
- Since there are only 4 possible outcomes (BB, BG, GB, GG), the probability that one pair is boys and the other is girls is (P(BG) + P(GB) = 1 (P(BB) + P(GG)) = 0.36). This can be split evenly between BG and GB, so each has a probability of 0.18.

We need to find the conditional probability that both are boys given that one of them is a boy. This is represented as \( P(BB|B) \).

Using Bayes' theorem:  $\Gamma(B|B) = \frac{P(B|BB)}{P(B)}$ 

Where:



- \( P(B|BB) \) is the probability that one of them is a boy given that both are boys, which is 1.
- \( P(BB) \) is the probability both are boys, which is 0.32.
- \( P(B) \) is the probability that at least one of them is a boy, which is \( P(BB) + P(BG) + P(GB) =  $0.32 + 0.18 + 0.18 = 0.68 \setminus$ .

So:

$$\Gamma(BB|B) = \frac{1 \times 0.32}{0.68} = \frac{0.32}{0.68} = 0.47$$

\*\*For the second question:\*\*

Given:

$$\begin{bmatrix} \phi'(x) = \phi(x) \end{bmatrix}$$
$$\begin{bmatrix} \phi(1) = 2 \end{bmatrix}$$

The above differential equation is a first-order ordinary differential equation (ODE) and its solution is:

$$[ \phi(x) = Ce^x ]$$

Using the boundary condition \(  $\phi(1) = 2 \$ \), we get: \[ 2 = Ce^1 \implies C = 2/e \]

So:

$$[ \varphi(x) = \frac{2x}{e} ]$$

When 
$$\ (x = \log_e(x) \):$$
  
\[ \phi(\log\_e x) = \frac{2 \log\_e x}{e} \]

From the options provided, none of them matches this exact expression.

However, if the question actually meant \( 
$$\phi(\log_e e)$$
 \) then: \[  $\phi(\log_e e) = \frac{2}{e} \]$ 

Answer for the second question:



Q: A photoelectric cell using cesium as the photosensitive element is illuminated with light of wavelength 4.2 X 10-7 m. The stopping potential is:

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1. 1.61 V
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4. 2.82 V

# Solution.

To determine the stopping potential, we use the photoelectric equation:

$$[eV_0 = h \frac{c}{\lambda} - \phi]$$

Where:

- \( V\_0 \) = stopping potential
- \( h \) = Planck's constant = \( 6.626 \times  $10^{-34}$  \) Js
- (c) = speed of light  $= (3 \times 10^8 )$  m/s
- \( \lambda \) = wavelength of light
- \(\phi\) = work function of the material (in this case, cesium)
- \( e \) = charge of an electron = \( 1.602 \times 10^{-19} \) C

Given:

$$[ \lambda = 4.2 \times 10^{-7} ] m$$

Substitute these values into the photoelectric equation:

$$[eV_0 = h \frac{c}{4.2 \times 10^{-7}} - 2.14 \times 1.602 \times 10^{-19}]$$

Solving for \( V\_0 \):

$$V_0 = \frac{h \times c}{4.2 \times 10^{-7} \times e} - 2.14$$



\[ V\_0 \approx 4.73 - 2.14 \]

\[ V\_0 \approx 2.59 \] V

\(  $V_0 \approx 2.59$ \) V is the stopping potential.

